
Parallel Processing

WS 2020/21

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3 Parallel Programming with Message Passing



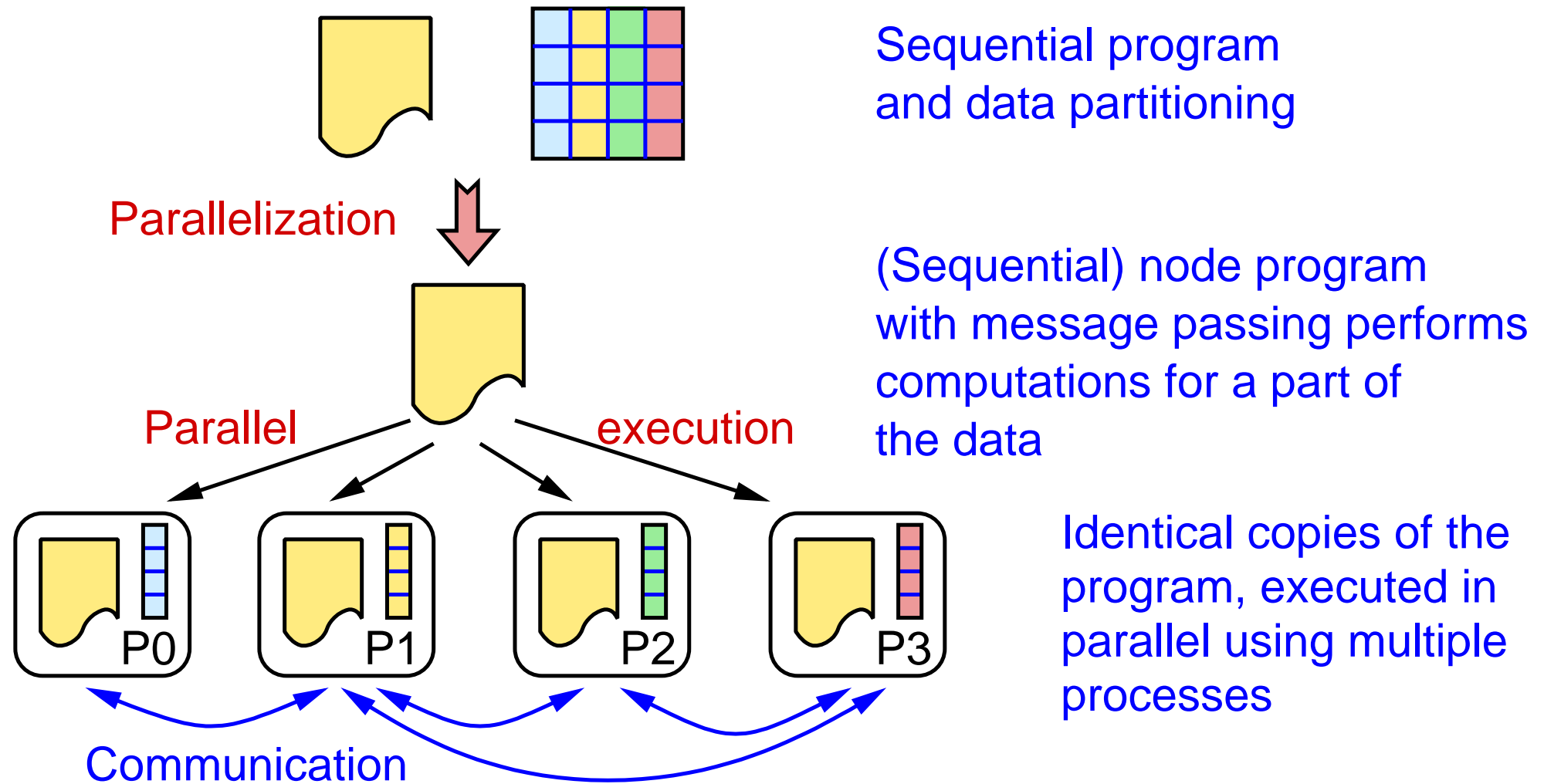
Contents

- ➔ Typical approach
- ➔ MPI (Message Passing Interface)
 - ➔ core routines
 - ➔ simple MPI programs
 - ➔ point-to-point communication
 - ➔ complex data types in messages
 - ➔ communicators
 - ➔ collective operations
 - ➔ further concepts

3.1 Typical approach



Data partitioning with SPMD model





Activities when creating a node program

- ➔ Adjustment of array declarations
 - ➔ node program stores only a part of the data
 - ➔ (assumption: data are stored in arrays)
- ➔ Index transformation
 - ➔ global index \leftrightarrow (process number, local index)
- ➔ Work partitioning
 - ➔ each process executes the computations on its part of the data
- ➔ Communication
 - ➔ when a process needs non-local data, a suitable message exchange must be programmed



About communication

- ➔ When a process needs data: the owner of the data must send them explicitly
 - ➔ exception: one-sided communication (👉 3.2.7)
- ➔ Communication should be merged as much as possible
 - ➔ one large message is better than many small ones
 - ➔ data dependences must not be violated

Sequential execution

```
a[1] = ...;  
a[2] = ...;  
a[3] = a[1]+...;  
a[4] = a[2]+...;
```

Parallel execution

Process 1

```
a[1] = ...;  
a[2] = ...;  
send(a[1],a[2]);
```

Process 2

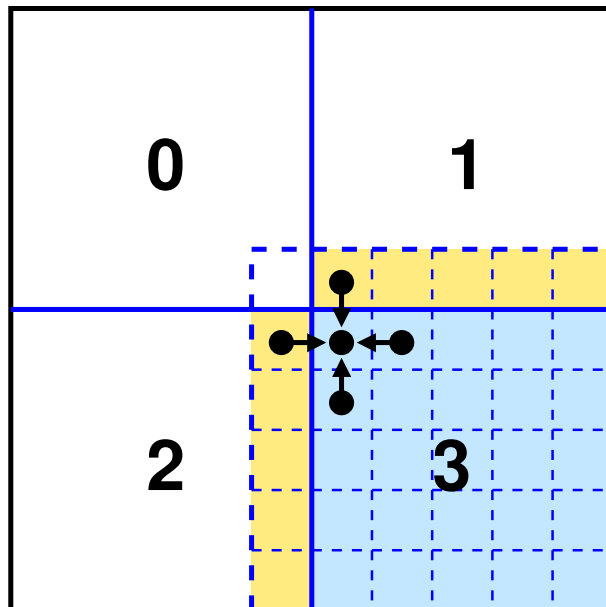
```
recv(a[1],a[2]);  
a[3] = a[1]+...;  
a[4] = a[2]+...;
```

3.1 Typical approach ...



About communication ...

- ➔ Often the node program allocates an overlapping buffer region (**ghost region** / **ghost cells**) for non-local data
- ➔ Example: Jacobi iteration



Partitioning of the matrix into 4 parts

Each process allocates an additional row/column at the borders of its sub-matrix

Data exchange at the end of each iteration



History and background

- ➔ At the beginning of the parallel computer era (late 1980's):
 - ➔ many different communication libraries (NX, PARMACS, PVM, P4, ...)
 - ➔ parallel programs are not easily portable
- ➔ Definition of an informal standard by the MPI forum
 - ➔ 1994: MPI-1.0
 - ➔ 1997: MPI-1.2 and MPI-2.0 (considerable extensions)
 - ➔ 2009: MPI 2.2 (clarifications, minor extensions)
 - ➔ 2012/15: MPI-3.0 und MPI-3.1 (considerable extensions)
 - ➔ documents at <http://www.mpi-forum.org/docs>
- ➔ MPI only defines the API (i.e., the programming interface)
 - ➔ different implementations, e.g., MPICH2, OpenMPI, ...



Programming model

- ➔ Distributed memory, processes with message passing
- ➔ SPMD: one program code for all processes
 - ➔ but different program codes are also possible
- ➔ MPI-1: static process model
 - ➔ all processes are created at program start
 - ➔ program start is standardized since MPI-2
 - ➔ MPI-2 also allows to create new processes at runtime
- ➔ MPI is thread safe: a process is allowed to create additional threads
 - ➔ hybrid parallelization using MPI and OpenMP is possible
- ➔ Program terminates when all its processes have terminated



- ➔ MPI-1.2 has 129 routines (and MPI-2 even more ...)
- ➔ However, often only 6 routines are sufficient to write relevant programs:
 - ➔ `MPI_Init` – MPI initialization
 - ➔ `MPI_Finalize` – MPI cleanup
 - ➔ `MPI_Comm_size` – get number of processes
 - ➔ `MPI_Comm_rank` – get own process number
 - ➔ `MPI_Send` – send a message
 - ➔ `MPI_Recv` – receive a message

MPI_Init

```
int MPI_Init(int *argc, char ***argv)
```

INOUT `argc` Pointer to `argc` of `main()`

INOUT `argv` Pointer to `argv` of `main()`

Result `MPI_SUCCESS` or error code

➔ Each MPI process must call `MPI_Init`, before it can use other MPI routines

➔ Typically:

```
int main(int argc, char **argv)
{
    MPI_Init(&argc, &argv);
    ...
}
```

➔ `MPI_Init` may also ensure that all processes receive the command line arguments



MPI_Finalize

```
int MPI_Finalize()
```

- ➔ Each MPI process must call `MPI_Finalize` at the end
- ➔ Main purpose: deallocation of resources
- ➔ After that, no other MPI routines must be used
 - ➔ in particular, no further `MPI_Init`
- ➔ `MPI_Finalize` does **not** terminate the process!



MPI_Comm_size

```
int MPI_Comm_size(MPI_Comm comm, int *size)
```

IN *comm* Communicator

OUT *size* Number of processes in *comm*

- ➔ Typically: `MPI_Comm_size(MPI_COMM_WORLD, &nprocs)`
 - ➔ returns the number of MPI processes in `nprocs`

MPI_Comm_rank

```
int MPI_Comm_rank(MPI_Comm comm, int *rank)
```

IN *comm* Communicator

OUT *rank* Number of processes in *comm*

- ➔ Process number (“rank”) counts upward, starting at 0
 - ➔ only differentiation of the processes in the SPMD model



Communicators

- ➔ A communicator consists of
 - ➔ a process group
 - ➔ a subset of all processes of the parallel application
 - ➔ a communication context
 - ➔ to allow the separation of different communication relations (👉 **3.2.5**)
- ➔ There is a predefined communicator `MPI_COMM_WORLD`
 - ➔ its process group contains all processes of the parallel application
- ➔ Additional communicators can be created as needed (👉 **3.2.5**)

MPI_Send

```
int MPI_Send(void *buf, int count, MPI_Datatype dtype,
             int dest, int tag, MPI_Comm comm)
```

<i>IN</i>	buf	(Pointer to) the data to be sent (send buffer)
<i>IN</i>	count	Number of data elements (of type dtype)
<i>IN</i>	dtype	Data type of the individual data elements
<i>IN</i>	dest	Rank of destination process in communicator comm
<i>IN</i>	tag	Message tag
<i>IN</i>	comm	Communicator

- ➔ Specification of data type: for format conversions
- ➔ Destination process is always relative to a communicator
- ➔ *Tag* allows to distinguish different messages (or message types) in the program



MPI_Send ...

- ➔ MPI_Send blocks the calling process, until all data has been read from the send buffer
 - ➔ send buffer can be reused (i.e., modified) immediately after MPI_Send returns
- ➔ The MPI implementation decides whether the process is blocked until
 - a) the data has been copied to a system buffer, or
 - b) the data has been received by the destination process.
 - ➔ in some cases, this decision can influence the correctness of the program! (👉 slide 286)



MPI_Recv

```
int MPI_Recv(void *buf, int count, MPI_Datatype dtype,
             int source, int tag, MPI_Comm comm,
             MPI_Status *status)
```

<i>OUT</i>	buf	(Pointer to) receive buffer
<i>IN</i>	count	Buffer size (number of data elements of type dtype)
<i>IN</i>	dtype	Data type of the individual data elements
<i>IN</i>	source	Rank of source process in communicator comm
<i>IN</i>	tag	Message tag
<i>IN</i>	comm	Communicator
<i>OUT</i>	status	Status (among others: actual message length)

➔ Process is blocked until the message has been completely received and stored in the receive buffer



MPI_Recv ...

- ➔ MPI_Recv only receives a message where
 - ➔ sender,
 - ➔ message tag, and
 - ➔ communicatormatch the parameters

- ➔ For source process (sender) and message tag, wild-cards can be used:
 - ➔ MPI_ANY_SOURCE: sender doesn't matter
 - ➔ MPI_ANY_TAG: message tag doesn't matter



MPI_Recv ...

- ➔ Message must not be larger than the receive buffer
 - ➔ but it may be smaller; the unused part of the buffer remains unchanged
- ➔ From the return value `status` you can determine:
 - ➔ the sender of the message: `status.MPI_SOURCE`
 - ➔ the message tag: `status.MPI_TAG`
 - ➔ the error code: `status.MPI_ERROR`
 - ➔ the actual length of the received message (number of data elements): `MPI_Get_count(&status, dtype, &count)`



Simple data types (MPI_Datatype)

MPI	C	MPI	C
MPI_CHAR	char	MPI_UNSIGNED_CHAR	unsigned char
MPI_SHORT	short	MPI_UNSIGNED_SHORT	unsigned short
MPI_INT	int	MPI_UNSIGNED	unsigned int
MPI_LONG	long	MPI_UNSIGNED_LONG	unsigned long
MPI_FLOAT	float		
MPI_DOUBLE	double	MPI_LONG_DOUBLE	long double
MPI_BYTE	Byte with 8 bits	MPI_PACKED	Packed data*

*  [3.2.4](#)

3.2.2 Simple MPI programs



Example: typical MPI program skeleton (👉 03/rahmen.cpp)

```
#include <iostream>
#include <mpi.h>
using namespace std;

int main (int argc, char **argv)
{
    int i;
    int myrank, nprocs;
    int namelen;
    char name[MPI_MAX_PROCESSOR_NAME];

    /* Initialize MPI and set the command line arguments */
    MPI_Init(&argc, &argv);

    /* Determine the number of processes */
    MPI_Comm_size(MPI_COMM_WORLD, &nprocs);
```

3.2.2 Simple MPI programs ...



```
/* Determine the own rank */
MPI_Comm_rank(MPI_COMM_WORLD, &myrank);

/* Determine the node name */
MPI_Get_processor_name(name, &namelen);

/* flush is used to enforce immediate output */
cout << "Process " << myrank << "/" << nprocs
     << "started on " << name << "\n" << flush;

cout << "-- Arguments: ";
for (i = 0; i<argc; i++)
    cout << argv[i] << " ";
cout << "\n";

/* finish MPI */
MPI_Finalize();

return 0;
}
```



Starting MPI programs: `mpiexec`

- ➔ `mpiexec -n 3 myProg arg1 arg2`
 - ➔ starts `myProg arg1 arg2` with 3 processes
 - ➔ the specification of the nodes to be used depends on the MPI implementation and the hardware/OS platform

- ➔ Starting the example program using MPICH:

```
mpiexec -n 3 -machinefile machines ./rahmen a1 a2
```

- ➔ Output:

```
Process 0/3 started on bslab02.lab.bvs
```

```
Args: /home/wismueller/LEHRE/pv/CODE/04/rahmen a1 a2
```

```
Process 2/3 started on bslab03.lab.bvs
```

```
Args: /home/wismueller/LEHRE/pv/CODE/04/rahmen a1 a2
```

```
Process 1/3 started on bslab06.lab.bvs
```

```
Args: /home/wismueller/LEHRE/pv/CODE/04/rahmen a1 a2
```

3.2.2 Simple MPI programs ...



Example: ping pong with messages (👉 03/pingpong.cpp)

```
int main (int argc, char **argv)
{
    int i, passes, size, myrank;
    char *buf;
    MPI_Status status;
    double start, end;

    MPI_Init(&argc, &argv);
    MPI_Comm_rank(MPI_COMM_WORLD, &myrank);

    passes = atoi(argv[1]); // Number of repetitions
    size = atoi(argv[2]); // Message length
    buf = new char[size];
```


3.2.2 Simple MPI programs ...



```
if (myrank == 0) {      /* Process 0 */
    start = MPI_Wtime(); // Get the current time
    for (i=0; i<passes; i++) {
        /* Send a message to process 1, tag = 42 */
        MPI_Send(buf, size, MPI_CHAR, 1, 42, MPI_COMM_WORLD);
        /* Wait for the answer, tag is not relevant */
        MPI_Recv(buf, size, MPI_CHAR, 1, MPI_ANY_TAG,
                 MPI_COMM_WORLD, &status);
    }
    end = MPI_Wtime(); // Get the current time
    cout << "Time for one message: "
          << ((end - start) * 1e6 / (2 * passes)) << "us\n";
    cout << "Bandwidth: "
          << (size*2*passes/(1024*1024*(end-start))) << "MB/s`
}
}
```

3.2.2 Simple MPI programs ...



```
else { /* Process 1 */  
    for (i=0; i<passes; i++) {  
        /* Wait for the message from process 0, tag is not relevant */  
        MPI_Recv(buf, size, MPI_CHAR, 0, MPI_ANY_TAG,  
                MPI_COMM_WORLD, &status);  
  
        /* Send back the answer to process 0, tag = 24 */  
        MPI_Send(buf, size, MPI_CHAR, 0, 24, MPI_COMM_WORLD);  
    }  
}  
  
MPI_Finalize();  
return 0;  
}
```

Example: ping pong with messages ...

➔ Results (on the XEON cluster):

➔ `mpiexec -n 2/pingpong 1000 1`
Time for one message: 50.094485 us
Bandwidth: 0.019038 MB/s

➔ `mpiexec -n 2/pingpong 1000 100`
Time for one message: 50.076485 us
Bandwidth: 1.904435 MB/s

➔ `mpiexec -n 2/pingpong 100 1000000`
Time for one message: 9018.934965 us
Bandwidth: 105.741345 MB/s

➔ (Only) with large messages the bandwidth of the interconnection network is reached

➔ XEON cluster: 1 GBit/s Ethernet ($\hat{=}$ 119.2 MB/s)

3.2.2 Simple MPI programs ...



Additional MPI routines in the examples:

```
int MPI_Get_processor_name(char *name, int *len)
```

OUT *name* Pointer to buffer for node name

OUT *len* Length of the node name

Result `MPI_SUCCESS` or error code

- ➔ The buffer for node name should have the length `MPI_MAX_PROCESSOR_NAME`

```
double MPI_Wtime()
```

Result Current wall clock time in seconds

- ➔ for timing measurements
- ➔ in MPICH2: time is synchronized between the nodes

3.2.3 Point-to-point communication



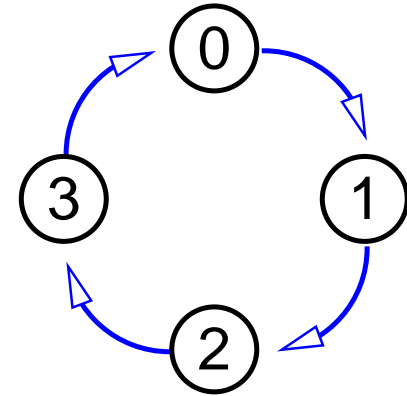
Example: sending in a closed cycle (👉 03/ring.cpp)

```
int a[N];
```

```
...
```

```
MPI_Send(a, N, MPI_INT, (myrank+1) % nprocs,  
         0, MPI_COMM_WORLD);
```

```
MPI_Recv(a, N, MPI_INT,  
        (myrank+nprocs-1) % nprocs,  
        0, MPI_COMM_WORLD, &status);
```



- ➔ Each process first attempts to send, before it receives
- ➔ This works **only if** MPI buffers the messages
- ➔ But MPI_Send can also block until the message is received
 - ➔ deadlock!

Example: sending in a closed cycle (correct)

➔ Some processes must first receive, before they send

```
int a[N];  
...  
if (myrank % 2 == 0) {  
    MPI_Send(a, N, MPI_INT, (myrank+1)%nprocs, ...  
    MPI_Recv(a, N, MPI_INT, (myrank+nprocs-1)%nprocs, ...  
}  
else {  
    MPI_Recv(a, N, MPI_INT, (myrank+nprocs-1)%nprocs, ...  
    MPI_Send(a, N, MPI_INT, (myrank+1)%nprocs, ...  
}
```

➔ Better: use non-blocking operations




Non-blocking communication

- ➔ `MPI_Isend` and `MPI_Irecv` return immediately
 - ➔ before the message actually has been sent / received
 - ➔ result: request object (`MPI_Request`)
 - ➔ send / receive buffer must not be modified / used, until the communication is completed
- ➔ `MPI_Test` checks whether communication is completed
- ➔ `MPI_Wait` blocks, until communication is completed
- ➔ Allows to overlap communication and computation
- ➔ can be “mixed” with blocking communication
 - ➔ e.g., send using `MPI_Send`, receive using `MPI_Irecv`

3.2.3 Point-to-point communication ...



Example: sending in a closed cycle with `MPI_Irecv`

( 03/ring2.cpp)

```
int sbuf[N];
```

```
int rbuf[N];
```

```
MPI_Status status;
```

```
MPI_Request request;
```

```
...
```

```
// Set up the receive request
```

```
MPI_Irecv(rbuf, N, MPI_INT, (myrank+nprocs-1) % nprocs, 0,  
          MPI_COMM_WORLD, &request);
```

```
// Sending
```

```
MPI_Send(sbuf, N, MPI_INT, (myrank+1) % nprocs, 0,  
         MPI_COMM_WORLD);
```

```
// Wait for the message being received
```

```
MPI_Wait(&request, &status);
```




- ➔ So far: only arrays can be send as messages
- ➔ What about complex data types (e.g., structures)?
 - ➔ z.B. `struct bsp { int a; double b[3]; char c; };`
- ➔ MPI offers two mechanisms
 - ➔ **packing and unpacking** the individual components
 - ➔ use `MPI_Pack` to pack components into a buffer one after another; send as `MPI_PACKED`; extract the components again using `MPI_Unpack`
 - ➔ **derived data types**
 - ➔ `MPI_Send` gets a pointer to the data structure as well as a description of the data type
 - ➔ the description of the data type must be created by calling MPI routines



Derived data types

- ➔ MPI offers constructors, which can be used to define own (derived) data types:
 - ➔ for contiguous data: `MPI_Type_contiguous`
 - ➔ allows the definition of array types
 - ➔ for non-contiguous data: `MPI_Type_vector`
 - ➔ e.g., for a column of a matrix or a sub-matrix
 - ➔ for structures: `MPI_Type_create_struct`
- ➔ After a new data type has been created, it must be “announced”:
`MPI_Type_commit`
- ➔ After that, the data type can be used like a predefined data type (e.g., `MPI_INT`)

MPI_Type_vector: **non-contiguous arrays**

```
int MPI_Type_vector(int count, int blocklen, int stride,
                   MPI_Datatype oldtype,
                   MPI_Datatype *newtype)
```

<i>IN</i>	count	Number of data blocks
<i>IN</i>	blocklen	Length of the individual data blocks
<i>IN</i>	stride	Distance between successive data blocks
<i>IN</i>	oldtype	Type of the elements in the data blocks
<i>OUT</i>	newtype	Newly created data type

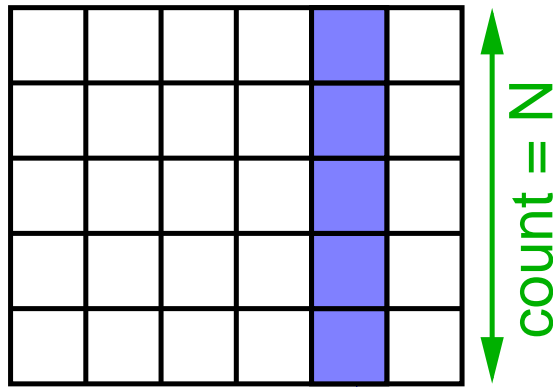
- ➔ Summarizes a number of data blocks (described as arrays) into a new data type
- ➔ However, the result is more like a new **view** onto the existing data than a new data **type**

3.2.4 Complex data types in messages ...



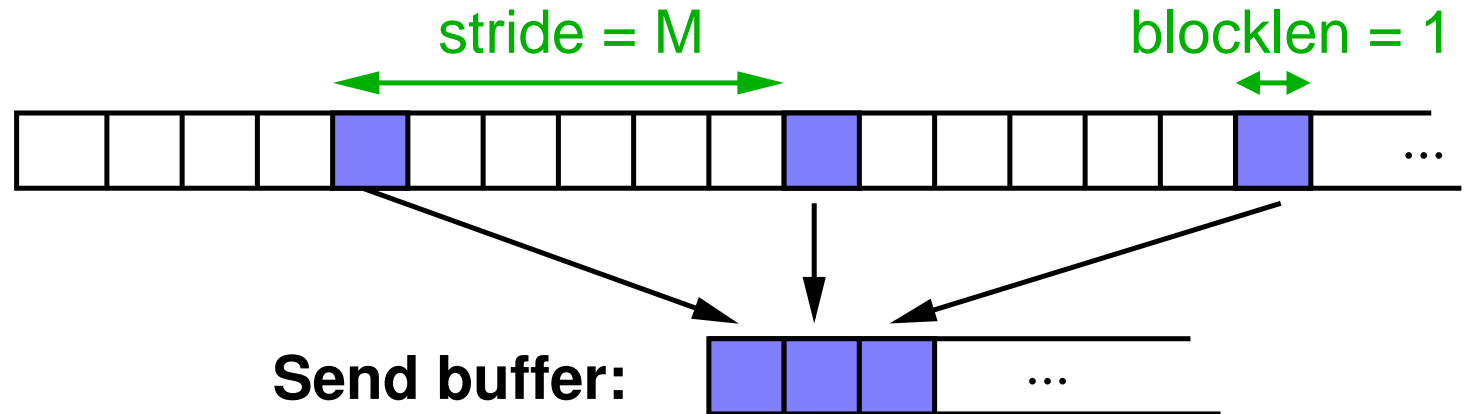
Example: transferring a column of a matrix

Matrix: $a[N][M]$



This column should be sent

Memory layout of the matrix:



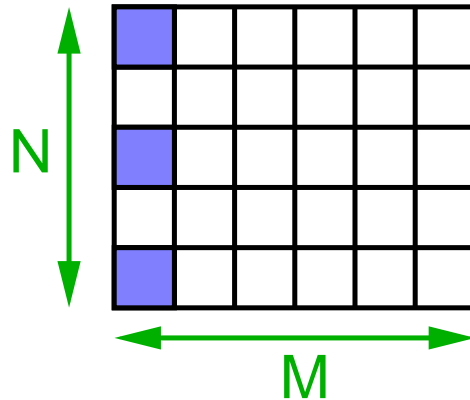
```
MPI_type_vector(N, 1, M, MPI_INT, &column);
MPI_Type_commit(&column);
// Transfer the column
if (rank==0) MPI_Send(&a[0][4], 1, column, 1, 0, comm);
else MPI_Recv(&a[0][4], 1, column, 0, 0, comm, &status);
```

3.2.4 Complex data types in messages ...

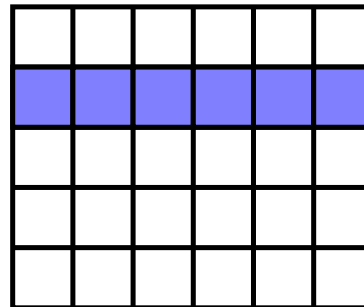


Additional options of MPI_Type_vector

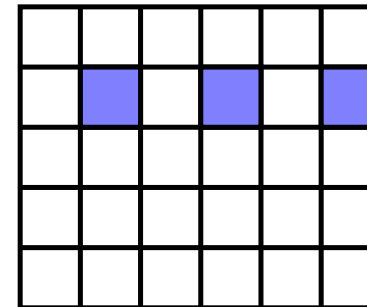
Every second
element of a
column



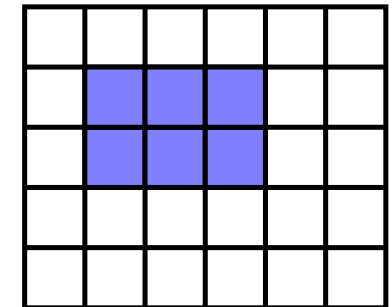
One
row



Every second
element of a
row



One
sub-
matrix



count	$N / 2$	1	M	$M / 2$	2
blocklen	1	M	1	1	3
stride	$2 * M$	x	1	2	M



Remarks on `MPI_Type_vector`

- ➔ The receiver can use a different data type than the sender
- ➔ It is only required that the number of elements and the sequence of their types is the same in the send and receive operations
- ➔ Thus, e.g., the following is possible:
 - ➔ sender transmits a column of a matrix
 - ➔ receiver stores it in a one-dimensional array

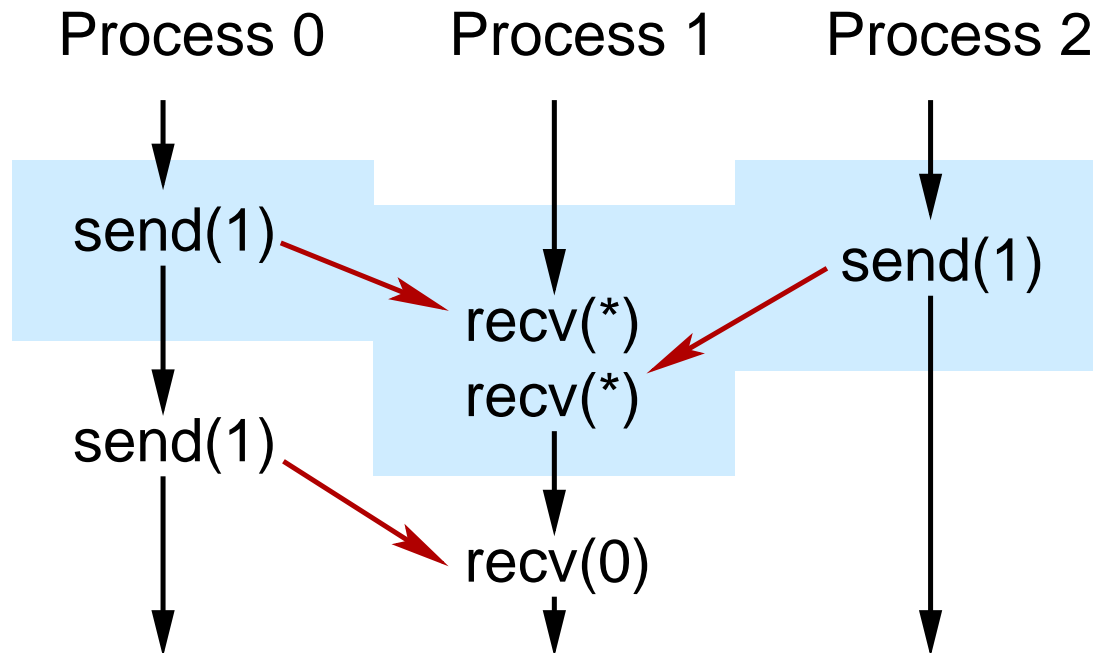
```
int a[N][M], b[N];  
MPI_type_vector(N, 1, M, MPI_INT, &column);  
MPI_Type_commit(&column);  
if (rank==0) MPI_Send(&a[0][4], 1, column, 1, 0, comm);  
else MPI_Recv(b, N, MPI_INT, 0, 0, comm, &status);
```



How to select the best approach

- ➔ Homogeneous data (elements of the same type):
 - ➔ contiguous (stride 1): standard data type and count parameter
 - ➔ non-contiguous:
 - ➔ stride is constant: `MPI_Type_vector`
 - ➔ stride is irregular: `MPI_Type_indexed`
- ➔ Heterogeneous data (elements of different types):
 - ➔ large data, often transmitted: `MPI_Type_create_struct`
 - ➔ few data, rarely transmitted: `MPI_Pack` / `MPI_Unpack`
 - ➔ structures of variable length: `MPI_Pack` / `MPI_Unpack`

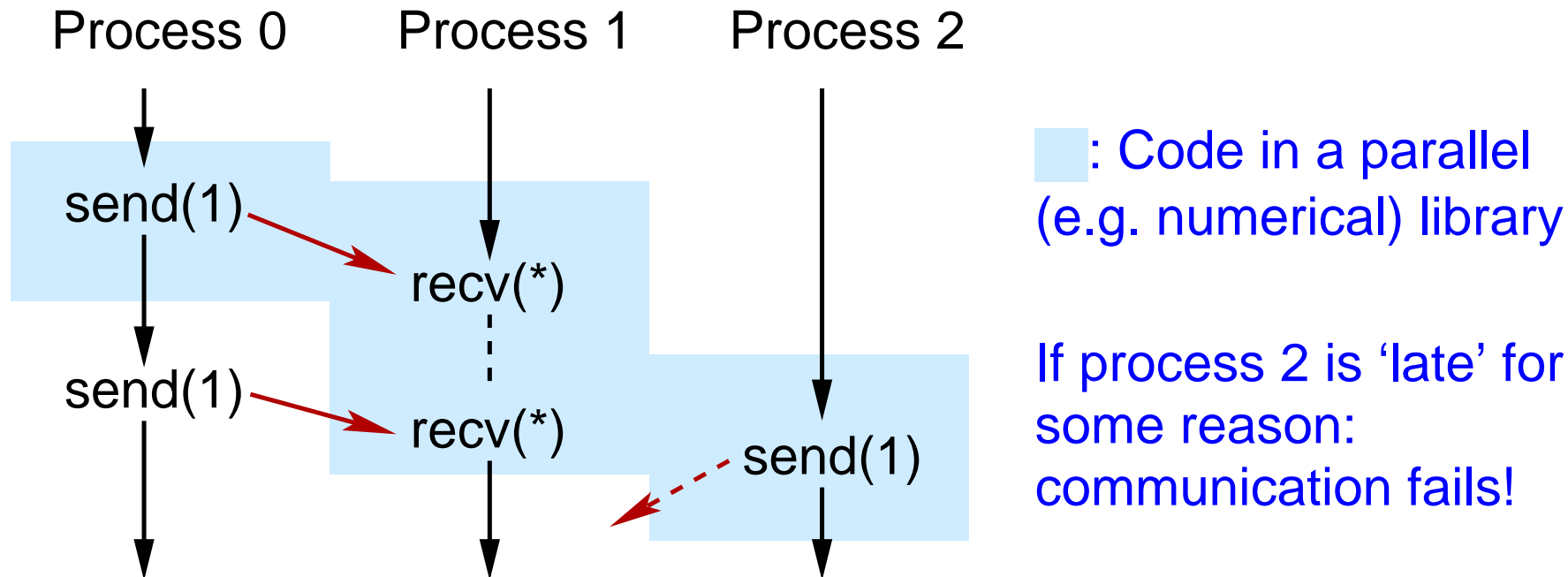
Motivation: problem of earlier communication libraries



■ : Code in a parallel (e.g. numerical) library

Process 1 should receive from 0 and 2 (in arbitrary order)

Motivation: problem of earlier communication libraries



- ➔ Message tags are not a reliable solution
 - ➔ tags might be chosen identically by chance!
- ➔ Required: different communication contexts

- ➔ Communicator = process group + context
- ➔ Communicators support
 - ➔ working with process groups
 - ➔ task parallelism
 - ➔ coupled simulations
 - ➔ collective communication with a subset of all processes
 - ➔ communication contexts
 - ➔ for parallel libraries
- ➔ A communicator represents a communication domain
 - ➔ communication is possible only within the same domain
 - ➔ no wild-card for communicator in `MPI_Recv`
 - ➔ a process can belong to several domains at the same time



Creating new communicators

```
int MPI_Comm_dup(MPI_Comm comm, MPI_Comm *newcomm)
int MPI_Comm_split(MPI_Comm comm, int color
                  int key, MPI_Comm *newcomm)
```

- ➔ Collective operations
 - ➔ all processes in `comm` must execute them concurrently
- ➔ `MPI_Comm_dup` creates a copy with a new context
- ➔ `MPI_Comm_split` splits `comm` into several communicators
 - ➔ one communicator for each value of `color`
 - ➔ as the result, each process receives the communicator to which it was assigned
 - ➔ `key` determines the order of the new process ranks

Example for MPI_Comm_split

- ➔ *Multi-physics code: air pollution*
 - ➔ one half of the processes computes the airflow
 - ➔ the other half computes chemical reactions
- ➔ Creation of two communicators for the two parts:

```
MPI_Comm_split(MPI_COMM_WORLD, myrank%2, myrank, &comm)
```

Process	myrank	Color	Result in comm	Rank in C_0	Rank in C_1
P0	0	0	C_0	0	—
P1	1	1	C_1	—	0
P2	2	0	C_0	1	—
P3	3	1	C_1	—	1



- ➔ Collective operations in MPI
 - ➔ must be executed concurrently by all processes of a process group (a communicator)
 - ➔ are blocking
 - ➔ do not necessarily result in a global (barrier) synchronisation, however
- ➔ Collective synchronisation and communication functions
 - ➔ barriers
 - ➔ communication: broadcast, scatter, gather, ...
 - ➔ reductions (communication with aggregation)

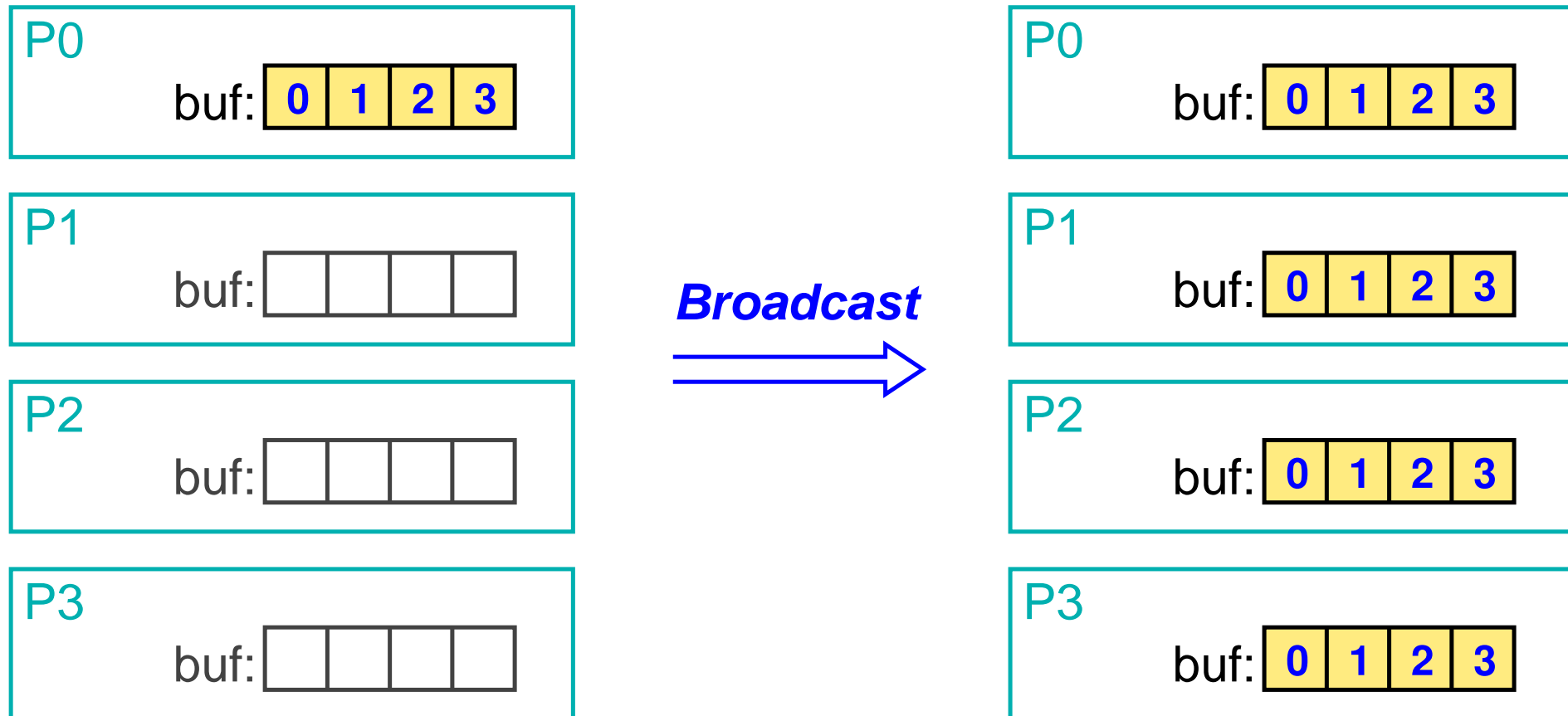


MPI_Barrier

```
int MPI_Barrier(MPI_Comm comm)
```

- ➔ Barrier synchronization of all processes in `comm`
- ➔ With message passing, barriers are actually not really necessary
 - ➔ synchronization is achieved by message exchange
- ➔ Reasons for barriers:
 - ➔ more easy understanding of the program
 - ➔ timing measurements, debugging output
 - ➔ console input/output ??
 - ➔ MPI-2: MPI I/O, one-sided communication

Collective communication: broadcast





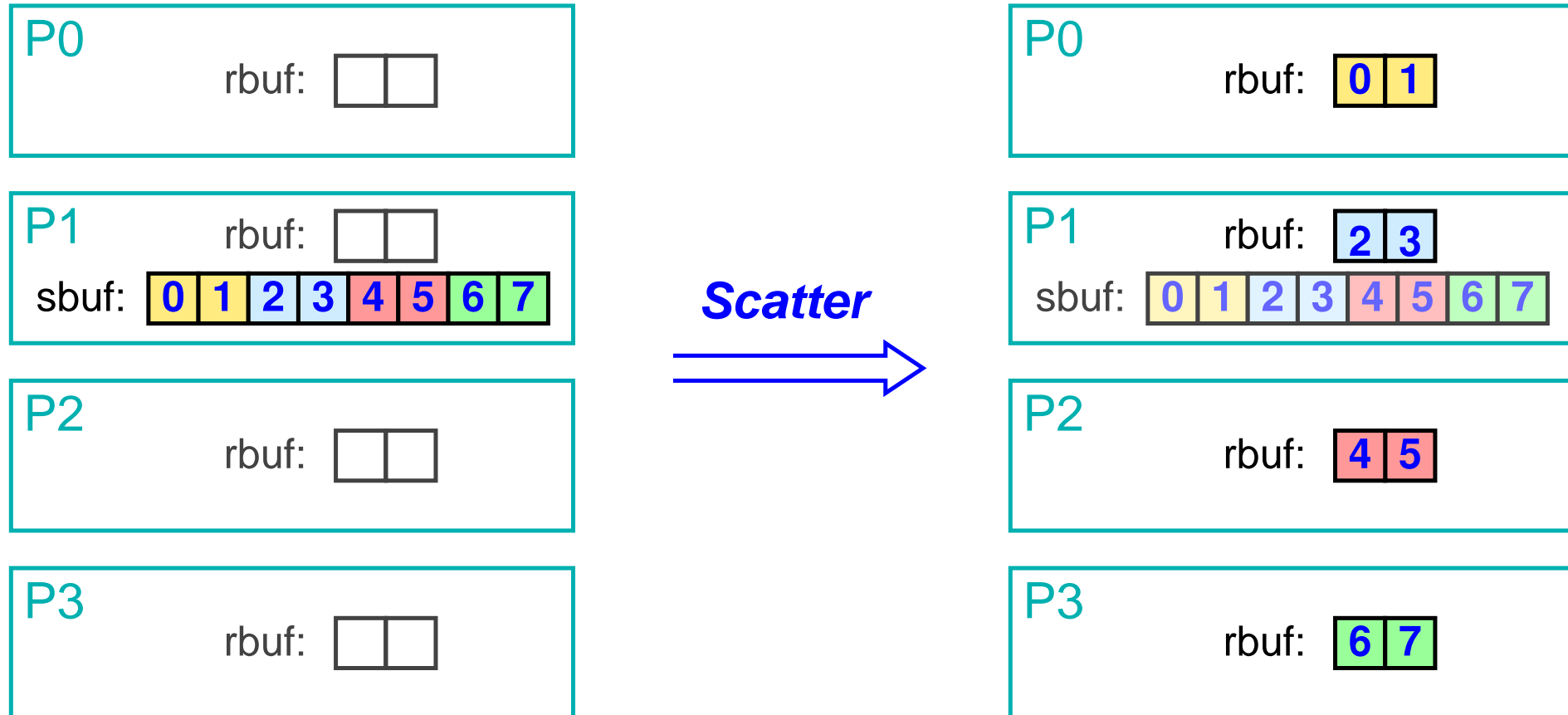
MPI_Bcast

```
int MPI_Bcast(void *buf, int count, MPI_Datatype dtype,  
             int root, MPI_Comm comm)
```

IN `root` Rank of the sending process

- ➔ Buffer is sent by process `root` and received by all others
- ➔ Collective, blocking operation: no tag necessary
- ➔ `count`, `dtype`, `root`, `comm` must be the same in all processes

Collective communication: scatter



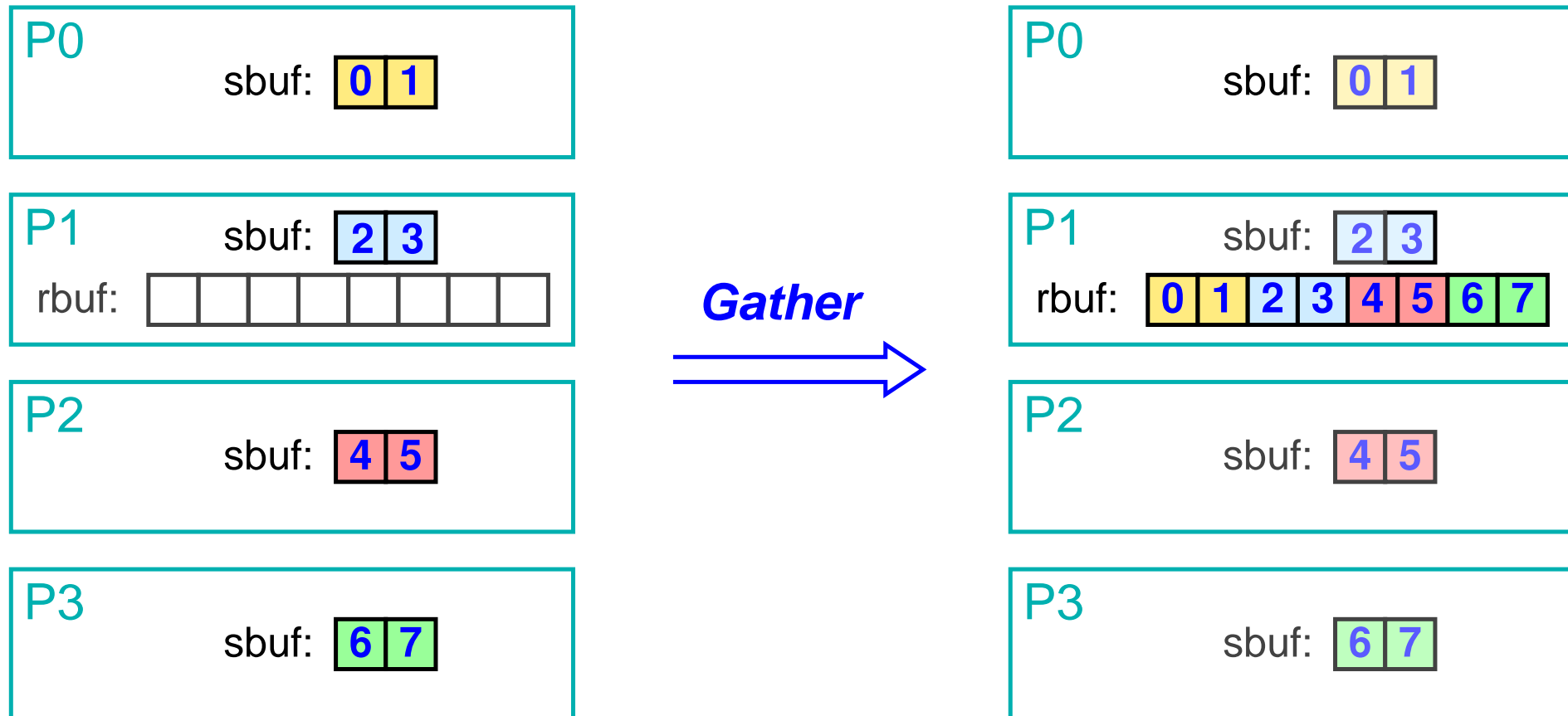


MPI_Scatter

```
int MPI_Scatter(void *sendbuf, int sendcount,
               MPI_Datatype sendtype,
               void *recvbuf, int recvcount,
               MPI_Datatype recvtype,
               int root, MPI_Comm comm)
```

- ➔ Process `root` sends a part of the data to each process
 - ➔ including itself
- ➔ `sendcount`: data length for each process (not the total length!)
- ➔ Process `i` receives `sendcount` elements of `sendbuf` starting from position $i * \text{sendcount}$
- ➔ Alternative `MPI_Scatterv`: length and position can be specified individually for each receiver

Collective communication: *Gather*



MPI_Gather

```
int MPI_Gather(void *sendbuf, int sendcount,
              MPI_Datatype sendtype,
              void *recvbuf, int recvcount,
              MPI_Datatype recvtype,
              int root, MPI_Comm comm)
```

- ➔ All processes send `sendcount` elements to process `root`
 - ➔ even `root` itself
- ➔ Important: each process must send the same amount of data
- ➔ `root` stores the data from process `i` starting at position $i * \text{recvcount}$ in `recvbuf`
- ➔ `recvcount`: data length for each process (not the total length!)
- ➔ Alternative `MPI_Gatherv`: analogous to `MPI_Scatterv`

3.2.6 Collective operations ...



Example: multiplication of vector and scalar (👉 03/vecmult.cpp)

```
double a[N], factor, local_a[LOCAL_N];
... // Process 0 reads a and factor from file
MPI_Bcast(&factor, 1, MPI_DOUBLE, 0, MPI_COMM_WORLD);
MPI_Scatter(a, LOCAL_N, MPI_DOUBLE, local_a, LOCAL_N,
           MPI_DOUBLE, 0, MPI_COMM_WORLD);
for (i=0; i<LOCAL_N; i++)
    local_a[i] *= factor;
MPI_Gather(local_a, LOCAL_N, MPI_DOUBLE, a, LOCAL_N,
           MPI_DOUBLE, 0, MPI_COMM_WORLD);
... // Process 0 writes a into file
```

➡ **Caution:** LOCAL_N must have the same value in all processes!

➡ otherwise: use MPI_Scatterv / MPI_Gatherv
(👉 03/vecmult3.cpp)

Reduction: MPI_Reduce

```
int MPI_Reduce(void *sendbuf, void *recvbuf,  
              int count, MPI_Datatype dtype,  
              MPI_Op op, int root,  
              MPI_Comm comm)
```

- ➔ Each element in the receive buffer is the result of a reduction operation (e.g., the sum) of the corresponding elements in the send buffer
- ➔ `op` defines the operation
 - ➔ predefined: minimum, maximum, sum, product, AND, OR, XOR, ...
 - ➔ in addition, user defined operations are possible, too

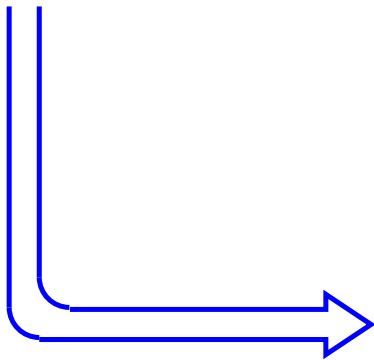
3.2.6 Collective operations ...



Example: summing up an array

Sequential

```
s = 0;
for (i=0;i<size;i++)
    s += a[i];
```



Parallel

```
local_s = 0;
for (i=0;i<local_size;i++)
    local_s += a[i];

MPI_Reduce(&local_s, &s,
           1, MPI_INT,
           MPI_SUM,
           0, MPI_COMM_WORLD);
```

More collective communication operations

- ➔ MPI_Alltoall: all-to-all broadcast (☞ 1.9.5)
- ➔ MPI_Allgather and MPI_Allgatherv: at the end, all processes have the gathered data
 - ➔ corresponds to a gather with subsequent broadcast
- ➔ MPI_Allreduce: at the end, all processes have the result of the reduction
 - ➔ corresponds to a reduce with subsequent broadcast
- ➔ MPI_Scan: prefix reduction
 - ➔ e.g., using the sum: process i receives the sum of the data from processes 0 up to and including i



- ➔ Topologies
 - ➔ the application's communication structure is stored in a communicator
 - ➔ e.g., cartesian grid
 - ➔ allows to simplify and optimize the communication
 - ➔ e.g., "send to the left neighbor"
 - ➔ the communicating processes can be placed on neighboring nodes
- ➔ Dynamic process creation (since MPI-2)
 - ➔ new processes can be created at run-time
 - ➔ process creation is a collective operation
 - ➔ the newly created process group gets its own `MPI_COMM_WORLD`
 - ➔ communication between process groups uses an *intercommunicator*



- ➔ One-sided communication (since MPI-2)
 - ➔ access to the address space of other processes
 - ➔ operations: read, write, atomic update
 - ➔ weak consistency model
 - ➔ explicit *fence* and *lock/unlock* operations for synchronisation
 - ➔ useful for applications with irregular communication
 - ➔ one process alone can execute the communication
- ➔ Parallel I/O (since MPI-2)
 - ➔ processes have individual views to a file
 - ➔ specified by an MPI data type
 - ➔ file operations: individual / collective, private / shared file pointer, blocking / non-blocking



- ➔ Basic routines:
 - ➔ `Init`, `Finalize`, `Comm_size`, `Comm_rank`, `Send`, `Recv`
- ➔ Complex data types in messages
 - ➔ `Pack` and `Unpack`
 - ➔ user defined data types
 - ➔ also for non-contiguous data (e.g., column of a matrix)
- ➔ Communicators: process group + communication context
- ➔ Non-blocking communication: `Isend`, `Irecv`, `Test`, `Wait`
- ➔ Collective operations
 - ➔ `Barrier`, `Bcast`, `Scatter(v)`, `Gather(v)`, `Reduce`, ...